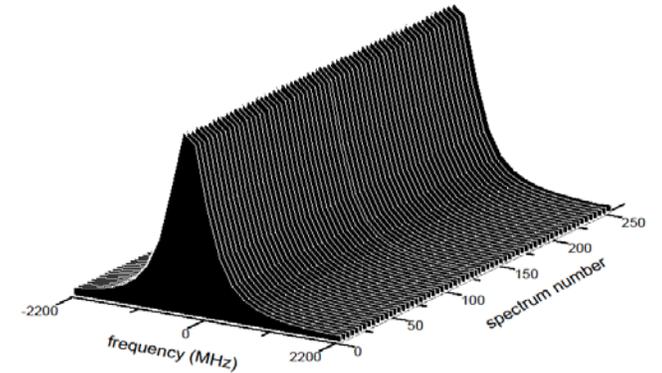


Quantitative Laser Spectroscopy for SI-Traceable Measurements of Greenhouse Gases

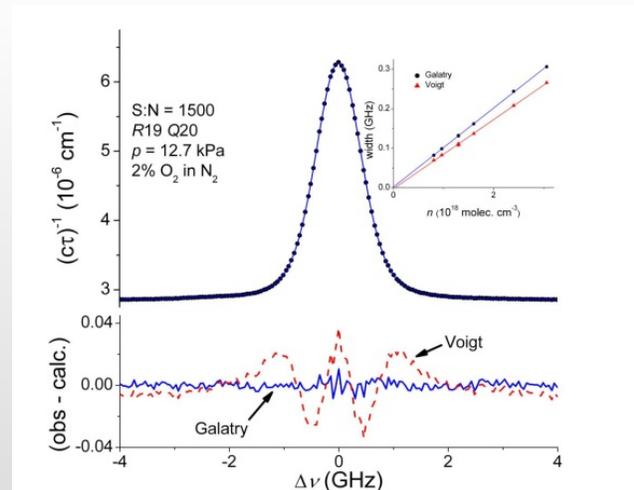
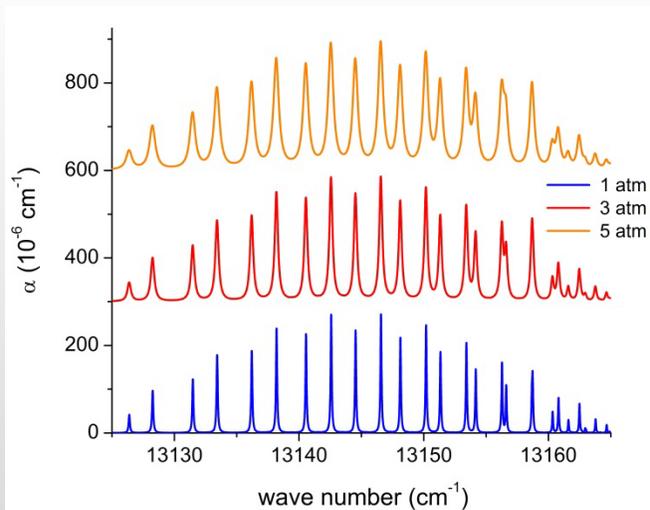
Joseph T. Hodges

Material Measurement Laboratory,
National Institute of Standards and Technology,
Gaithersburg, MD

joseph.hodges@nist.gov



250 spectra in 0.7 s



NOAA Global Monitoring Conference,
Boulder, CO; May 19-20, 2015

Outline

Line intensities as intrinsic standards for measurement of concentration

Frequency-stabilized cavity ring-down spectroscopy (FS-CRDS)

Comparison of measured and *ab initio* intensities for CO₂

Line shape effects

Development of mid-IR laser spectrometer for measuring ¹⁶O¹⁴C¹⁶O at natural abundance

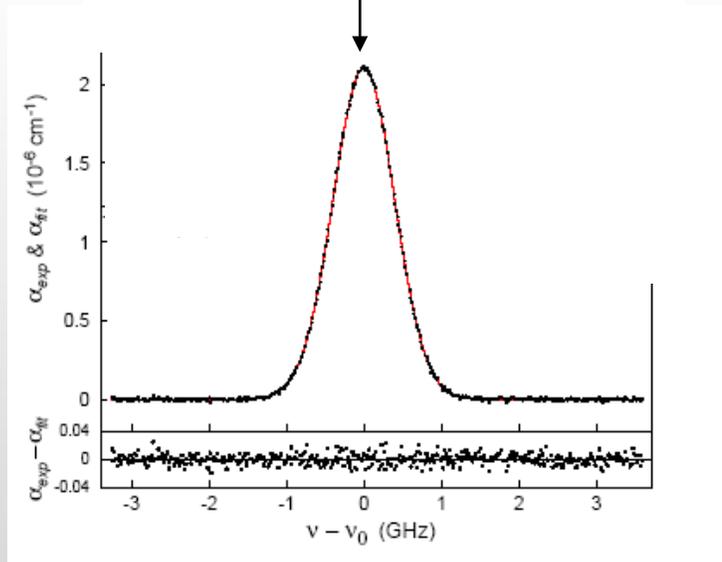
Measurement of Line Intensity (S) and Absorber Concentration (n)

$$S = \int \alpha(\nu) d\nu / \{ n \int g(\nu) d\nu \} = A/n$$

measured
absorption coefficient

line profile
(unity area)

fitted spectrum area



Once the intrinsic property S is known, then

$$n = A/S$$

Quantum (*ab initio*) calculation of line intensity, S_{12}

$$\mu_{12} = \int \Psi_1 \underline{\mu} \Psi_2 d\tau$$

Transition dipole

initial wavefunction
dipole moment surface (DMS)
final wavefunction
nuclear coordinates

$$S_{12} = \text{fn}(T) * |\mu_{12}|^2$$

Boltzmann factor

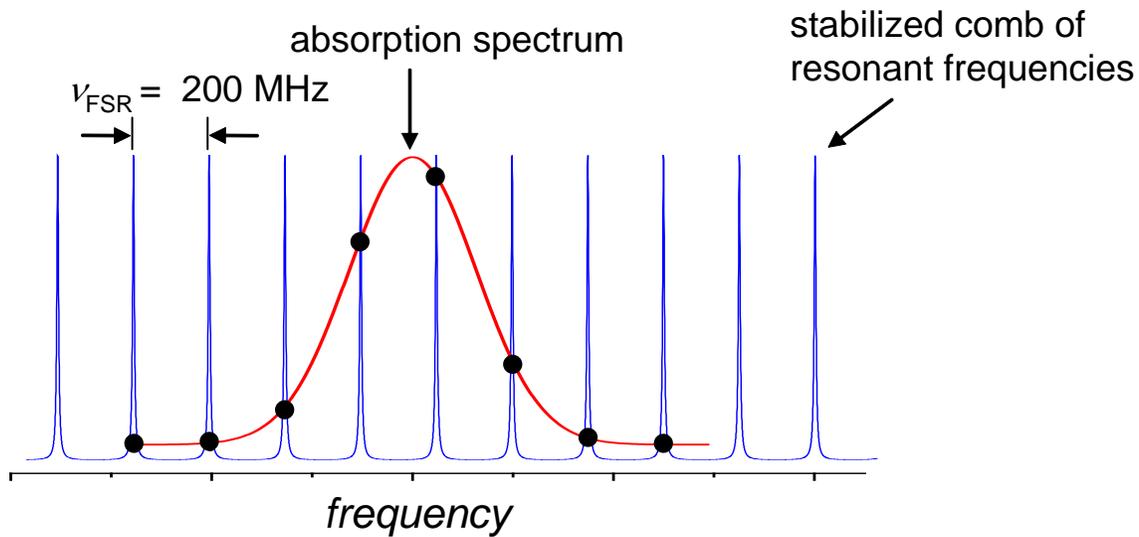
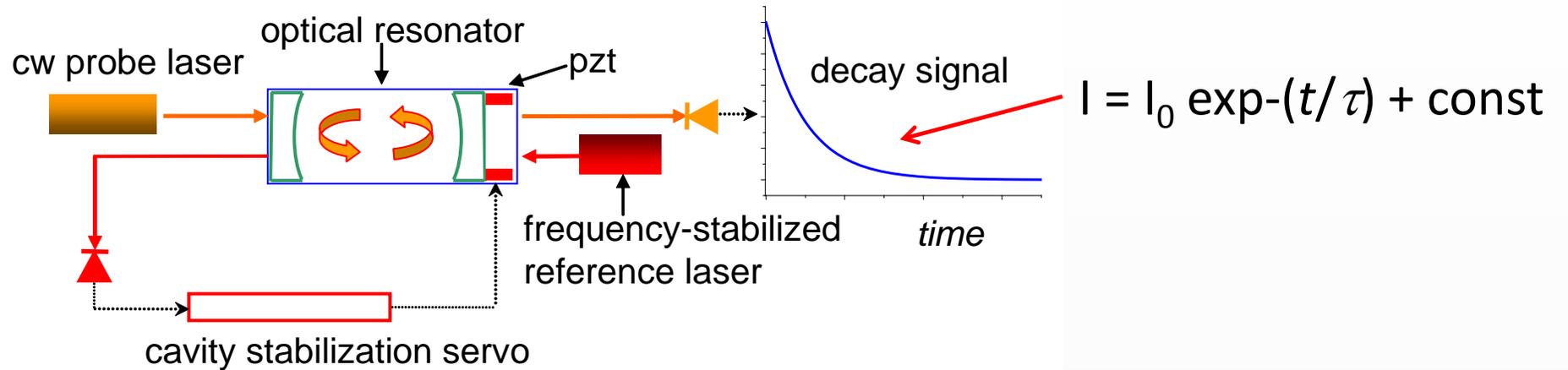
H₂O: 10-electron system
CO₂ 22-electron system

Calculation of S_{12} requires wave functions that are computed from potential energy surface (PES) and dipole moment surface (DMS)



O. Polyansky & J. Tennyson, University College of London

Frequency-stabilized cavity ring-down spectroscopy (FS-CRDS)



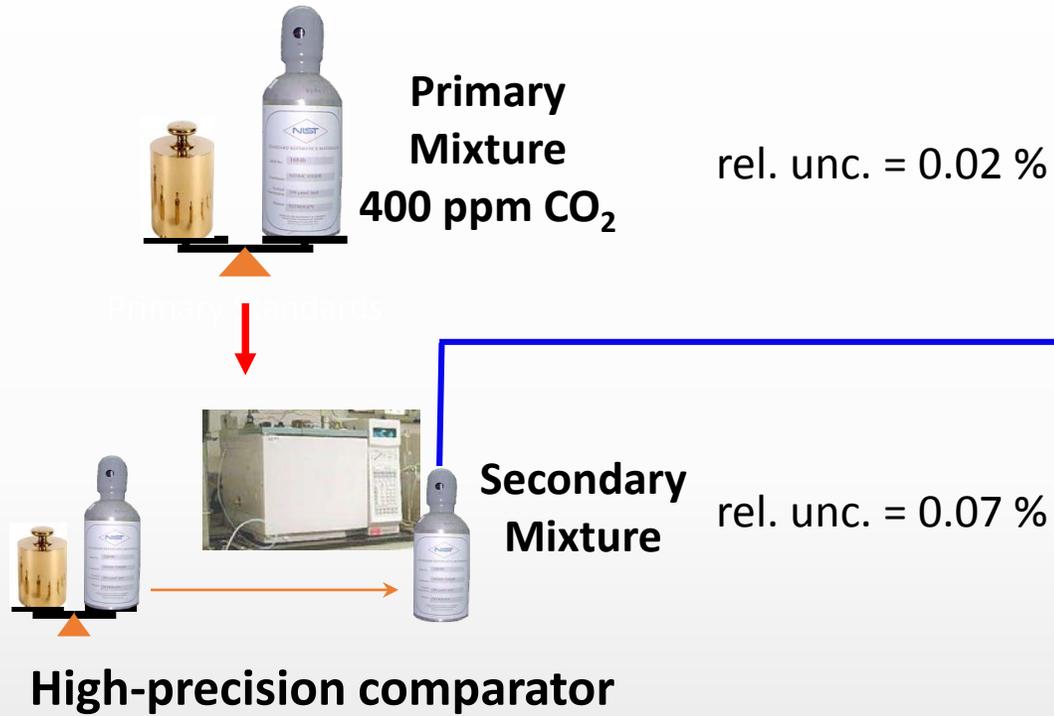
$$1/(c \tau) = \alpha_0 + \alpha(\nu)$$

time

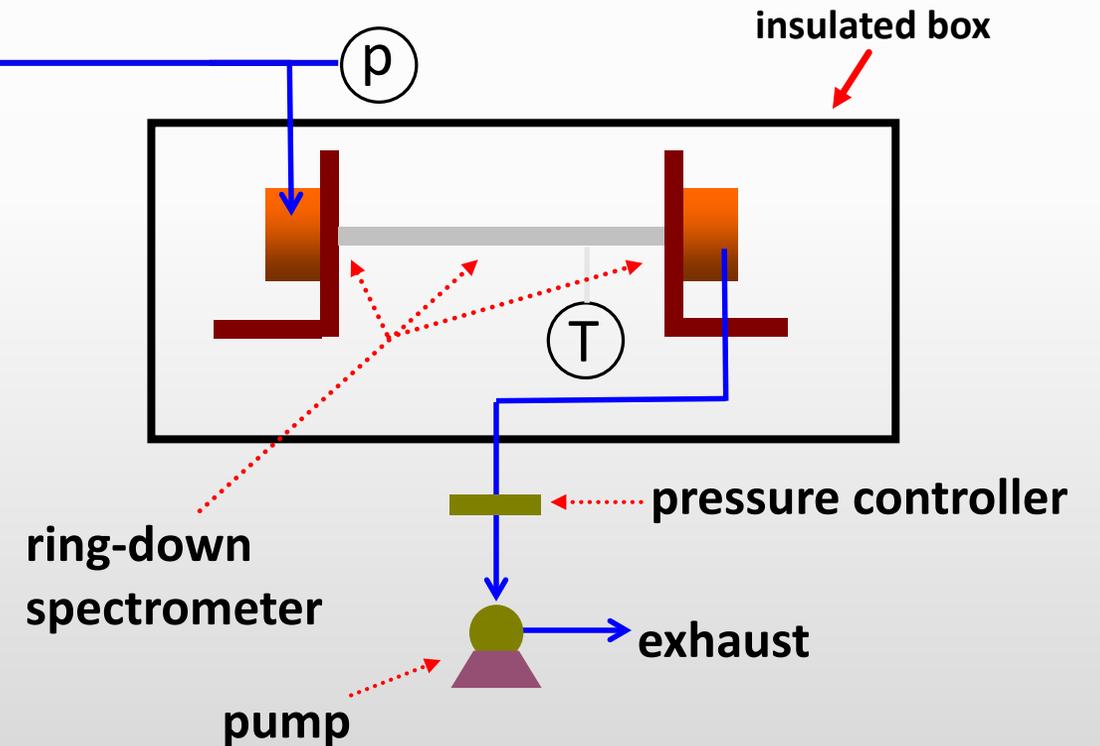
frequency

Enables high-fidelity and high-sensitivity measurements of transition areas, widths & shapes, positions and pressure shifts

CO₂-in-air sample preparation



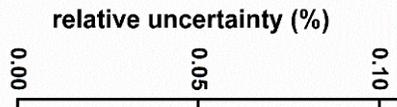
Need steady flow of sample gas to mitigate wall effects



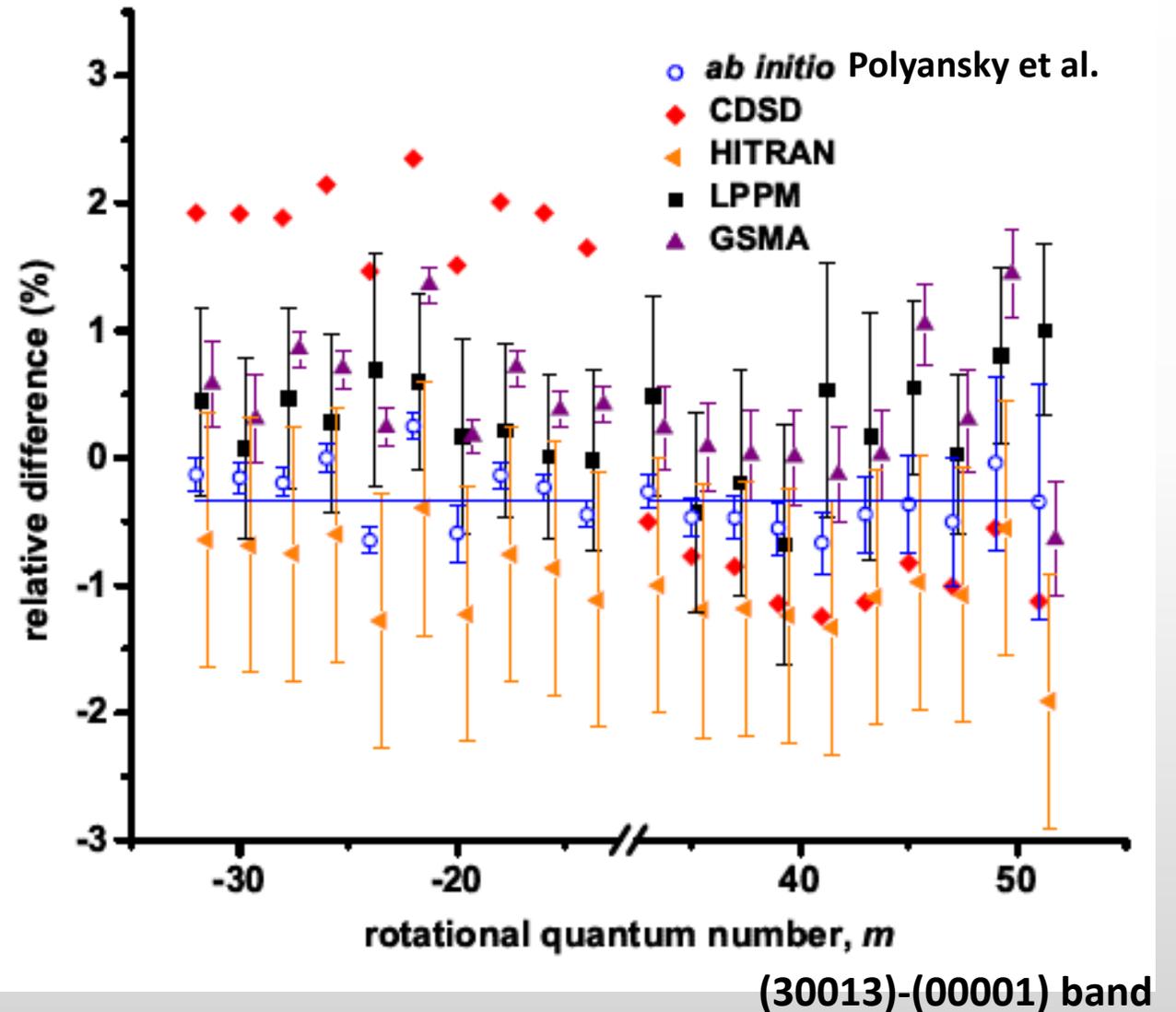
Accuracy of CO₂ intensity measurements: 1.6 um region

Polyansky et al., *High accuracy CO₂ line intensities from theory and experiment*, (under review)

uncertainties



- fit + residual area
- isotopic composition
- etalon
- T, p, mole fraction
- Total (quadrature sum)



Partially correlated quadratic-speed-dependent Nelkin-Ghatak Profile (aka “Hartmann-Tran” profile)

$$\tilde{I}_{\text{pCqSDNG}} = \frac{\tilde{I}_{\text{qSDV}}(u; B_w \Gamma_0 / \omega_D + \tilde{z})}{1 - \pi \tilde{z} \tilde{I}_{\text{qSDV}}(u; B_w \Gamma_0 / \omega_D + \tilde{z})} \quad \text{Complex profile}$$

$$\tilde{z} = \tilde{\nu}_{\text{opt}} / \omega_D = [\nu_{\text{eff}} - \eta(\Gamma_0 + i\Delta_0)] / \omega_D \quad \text{Complex, normalized narrowing frequency}$$

$$B_w(x) = 1 + a_w(x^2 - 3/2)$$

$$B_s(x) = 1 + a_s(x^2 - 3/2)$$

Quadratic approximation
to speed dependence

Correspondence between pCqSDHCP
and pCqSDNGP parameters

$$a_w = \Gamma_2 / \Gamma_0$$

$$a_s = \Delta_2 / \Delta_0$$

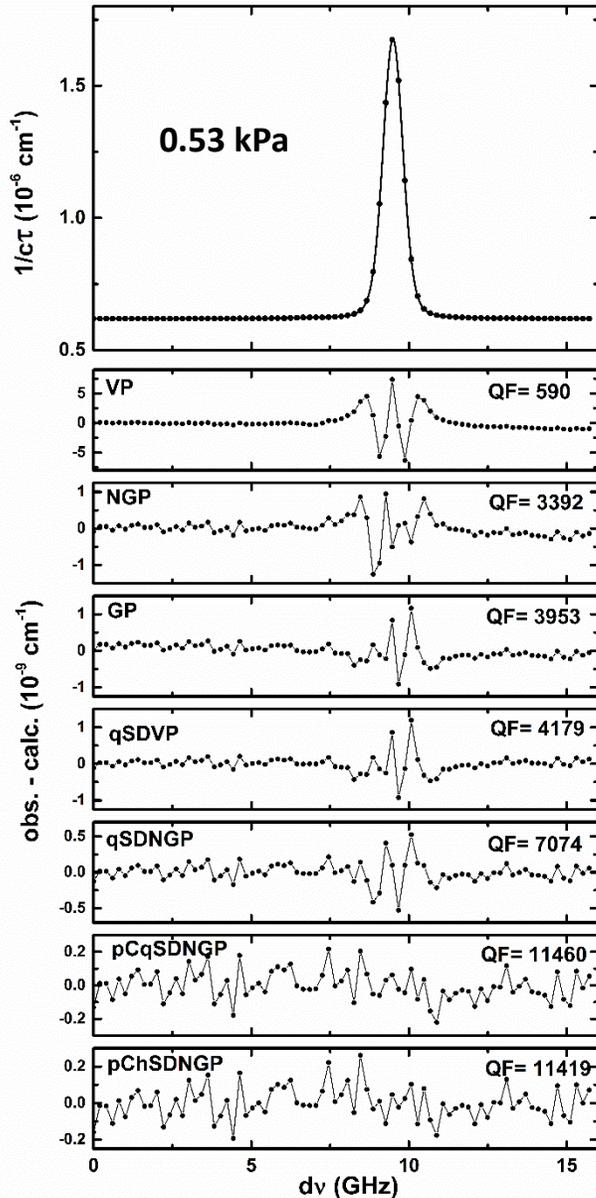
$$\text{Re}[\tilde{\nu}_{\text{opt}}] = \nu_{\text{vc}} - \eta\Gamma_0$$

$$\text{Im}[\tilde{\nu}_{\text{opt}}] = -\eta\Delta_0$$

Mechanisms: 1) collisional narrowing (hard-collision model), 2) speed-dependent broadening and shifting, 3) partial correlations between velocity-changing and dephasing collisions

H₂O line shape study

single-spectrum fit



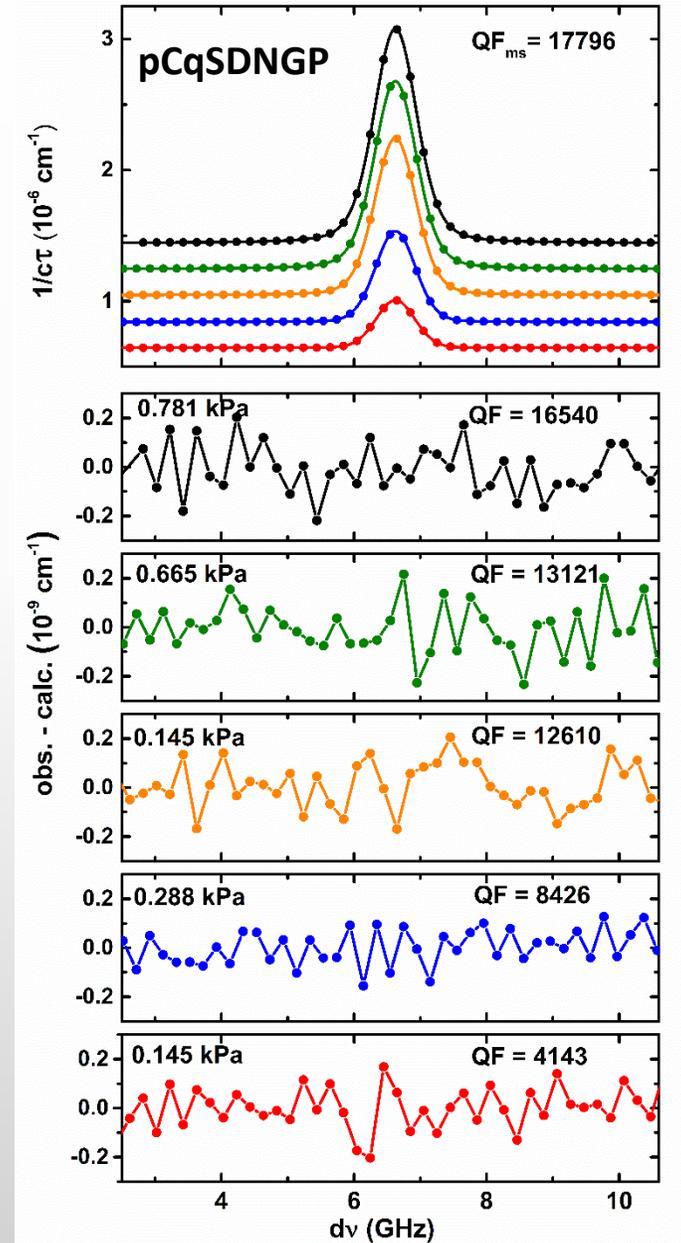
Need to include:

1. collisional narrowing
2. speed dependent effects
3. partial correlation between velocity-changing and dephasing collisions

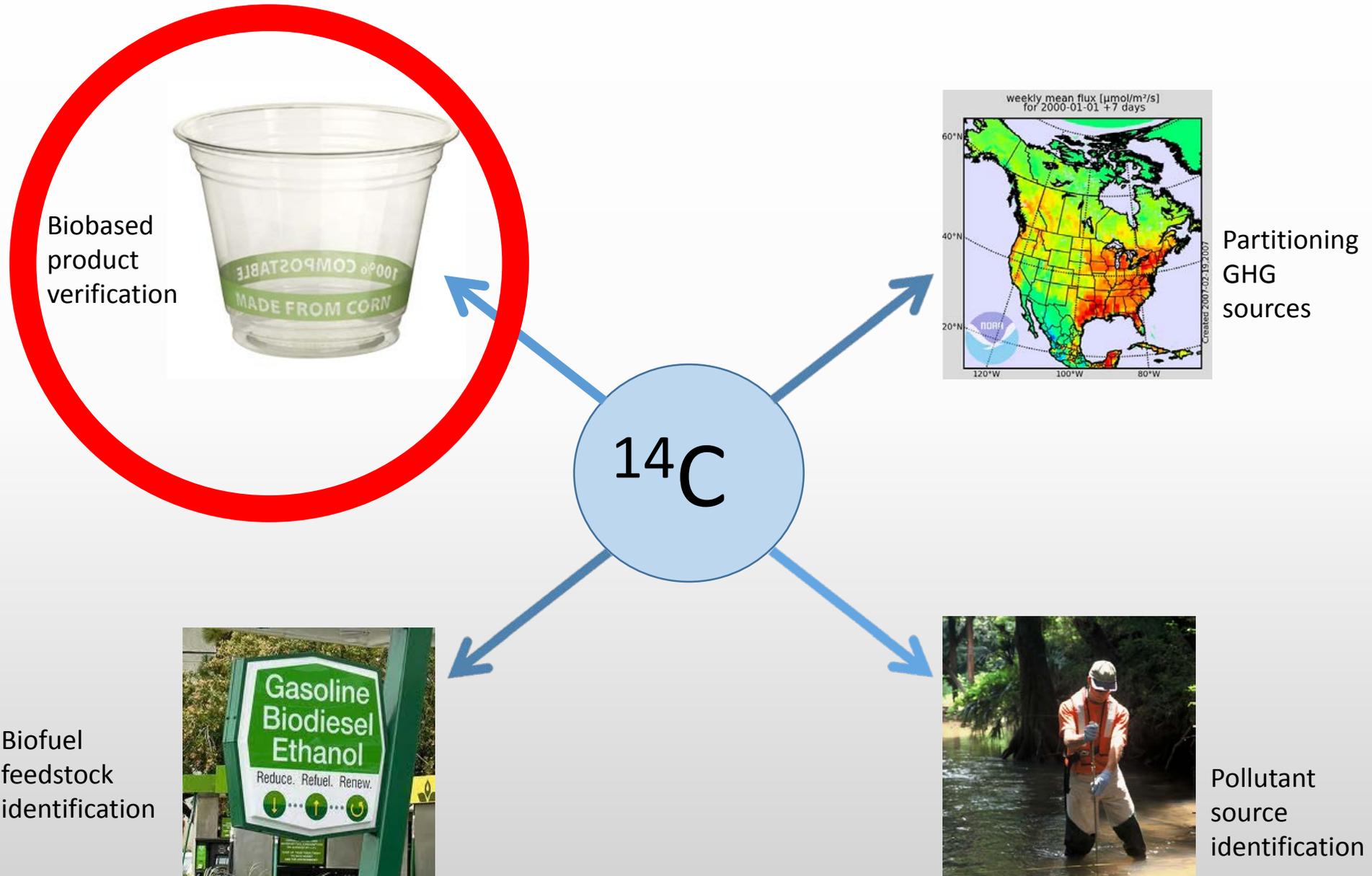
7892.3021 cm⁻¹
 $S = 1.89 \times 10^{-25} \text{ cm molec.}^{-1}$
 (002) - (000)
 (15 5 6) - (9 2 7): Q' - Q''

7799.9970 cm⁻¹
 $S = 2.58 \times 10^{-25} \text{ cm molec.}^{-1}$
 (002) - (000)
 (10 4 6) - (9 3 7): Q' - Q''

multi-spectrum fit



^{14}C : A tool for identifying the origins of feedstocks and emissions



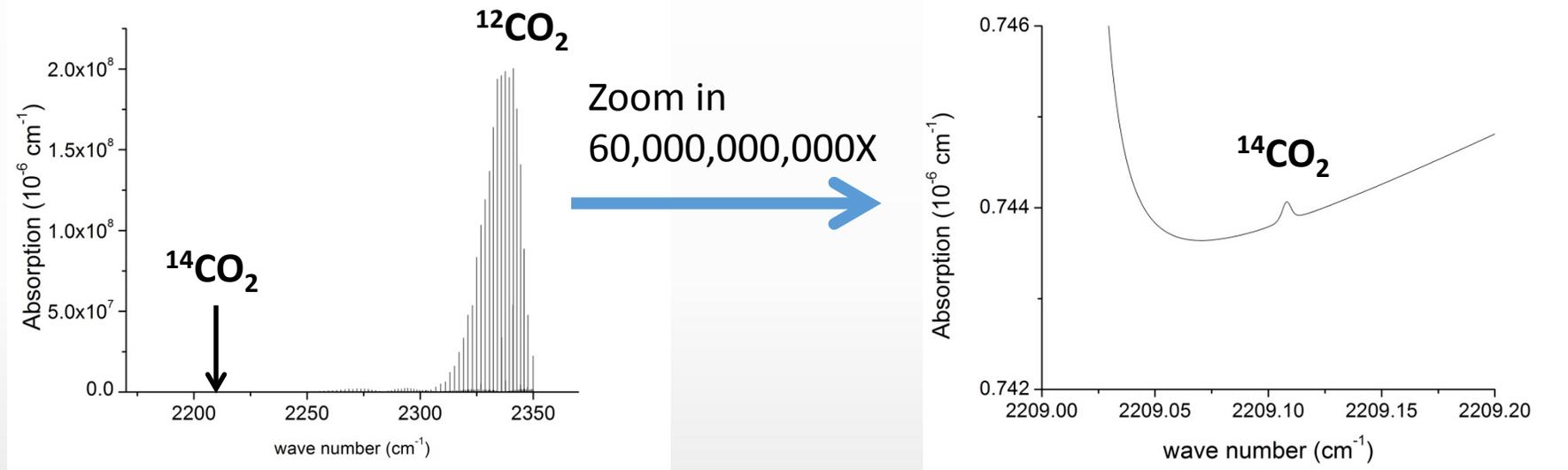
Current method: Accelerator mass spectrometry (AMS)

- Measurements of ^{14}C are extremely difficult due to low natural abundance (~ 1 ppt)
- AMS uses an accelerator to mass separate the analyte
- Then analyzed using mass spectrometry
- Disadvantages:
 - Expensive (\$6M/facility)
 - Requires a large facility and highly trained staff
 - Only 10 facilities in the U.S.
15-30 day lead time



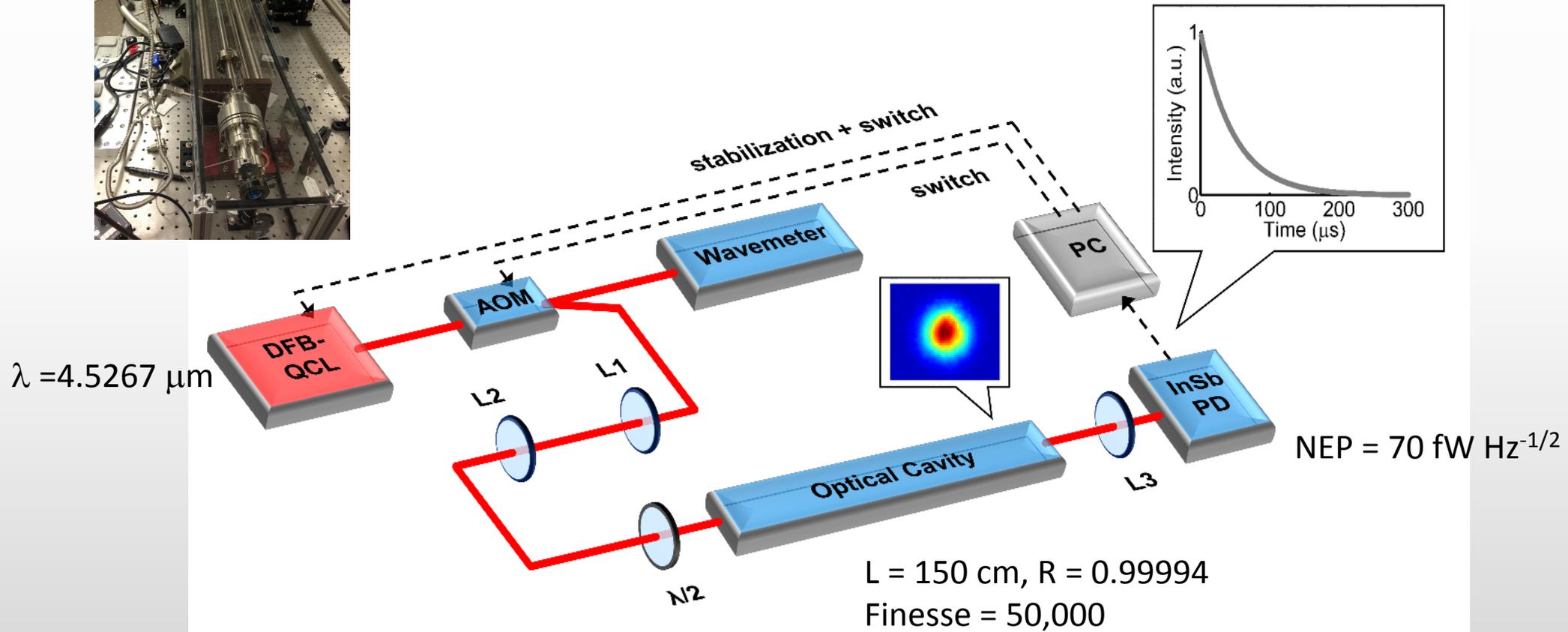
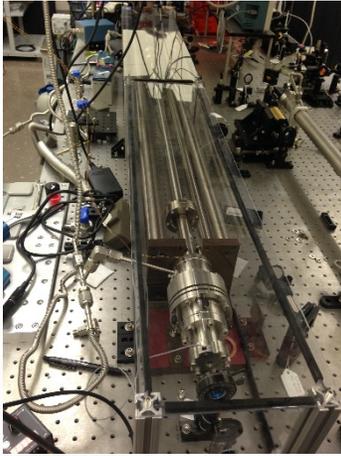
Optical measurements of $^{14}\text{CO}_2$

- $^{14}\text{CO}_2$ transitions are shifted relative to $^{12}\text{CO}_2$
 - Allows for spectroscopic measurements of $^{14}\text{CO}_2$ in the mid-infrared



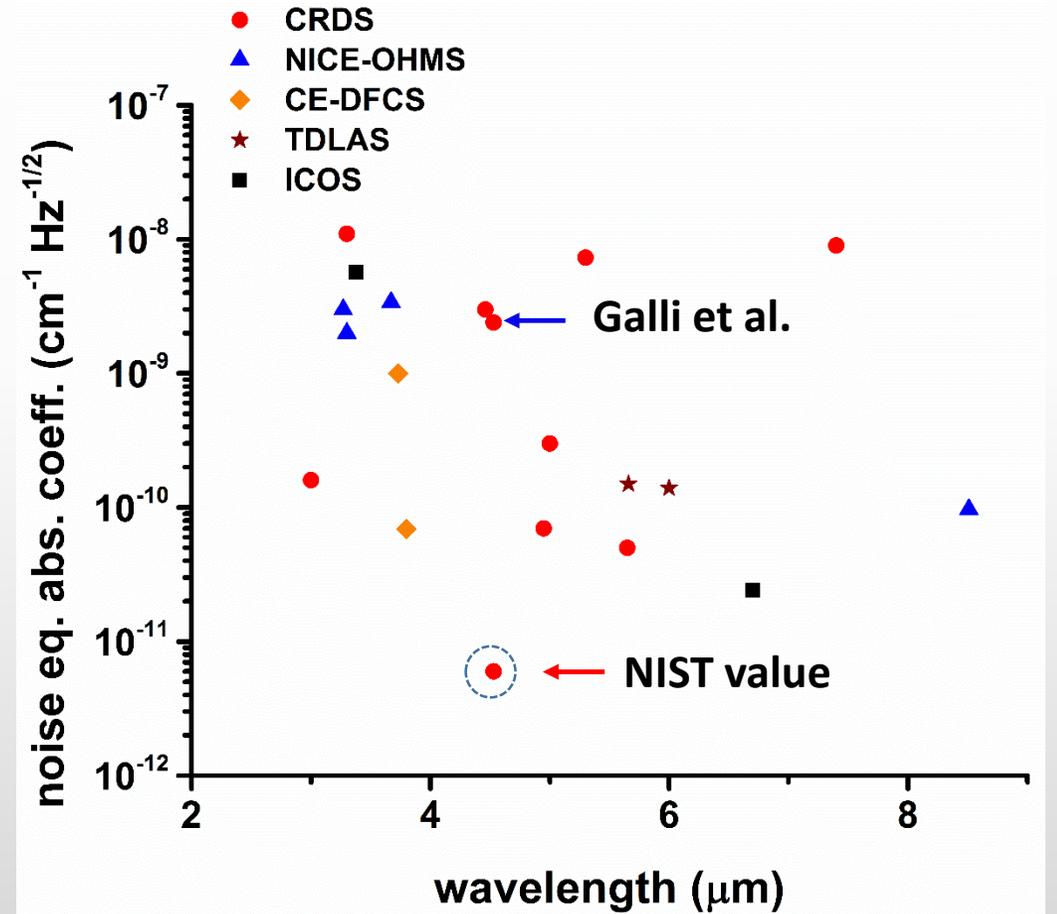
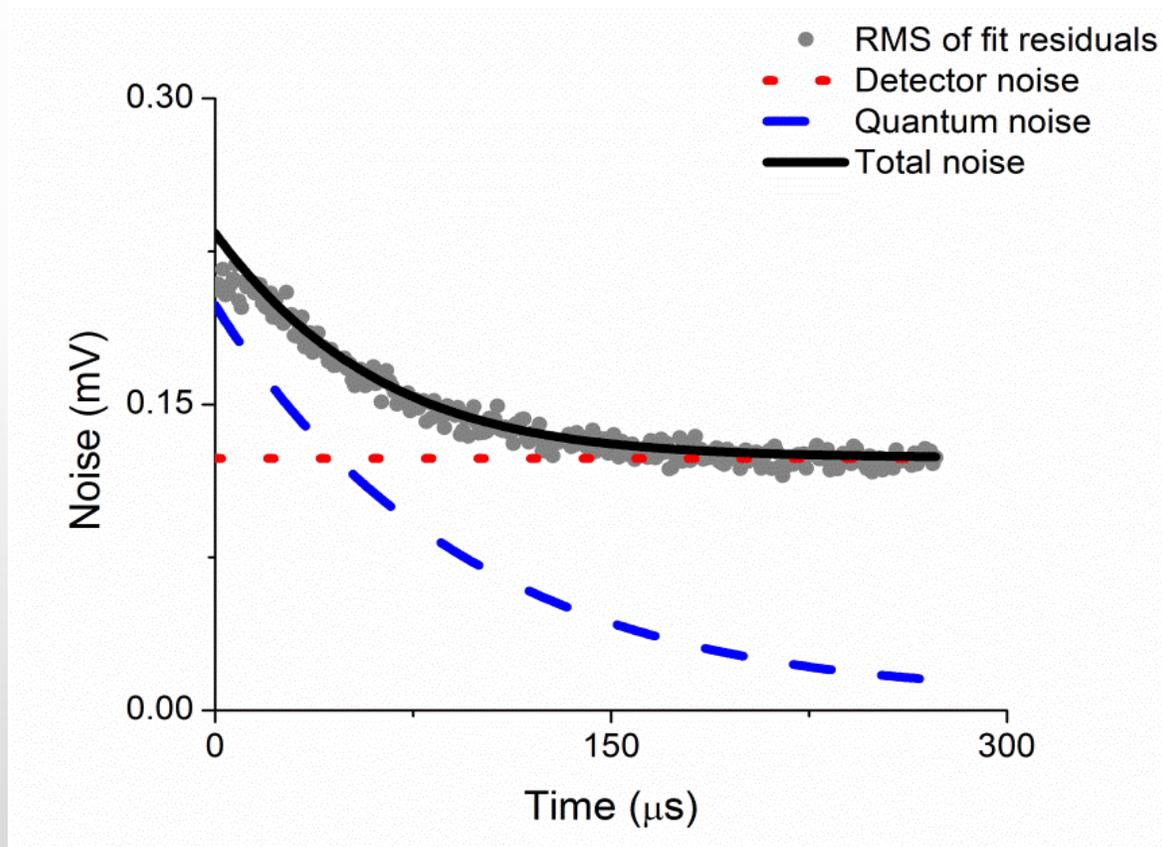
Because of the ultralow abundance of $^{14}\text{CO}_2$ (1.2 ppt) optical detection has only recently been demonstrated in the laboratory [Galli et al. PRL v107, 270802 (2011)] using a spectrometer at 195 K.

Mid-IR spectrometer for measuring ^{14}C at natural abundance



Ultra-high sensitivity in mid-IR region

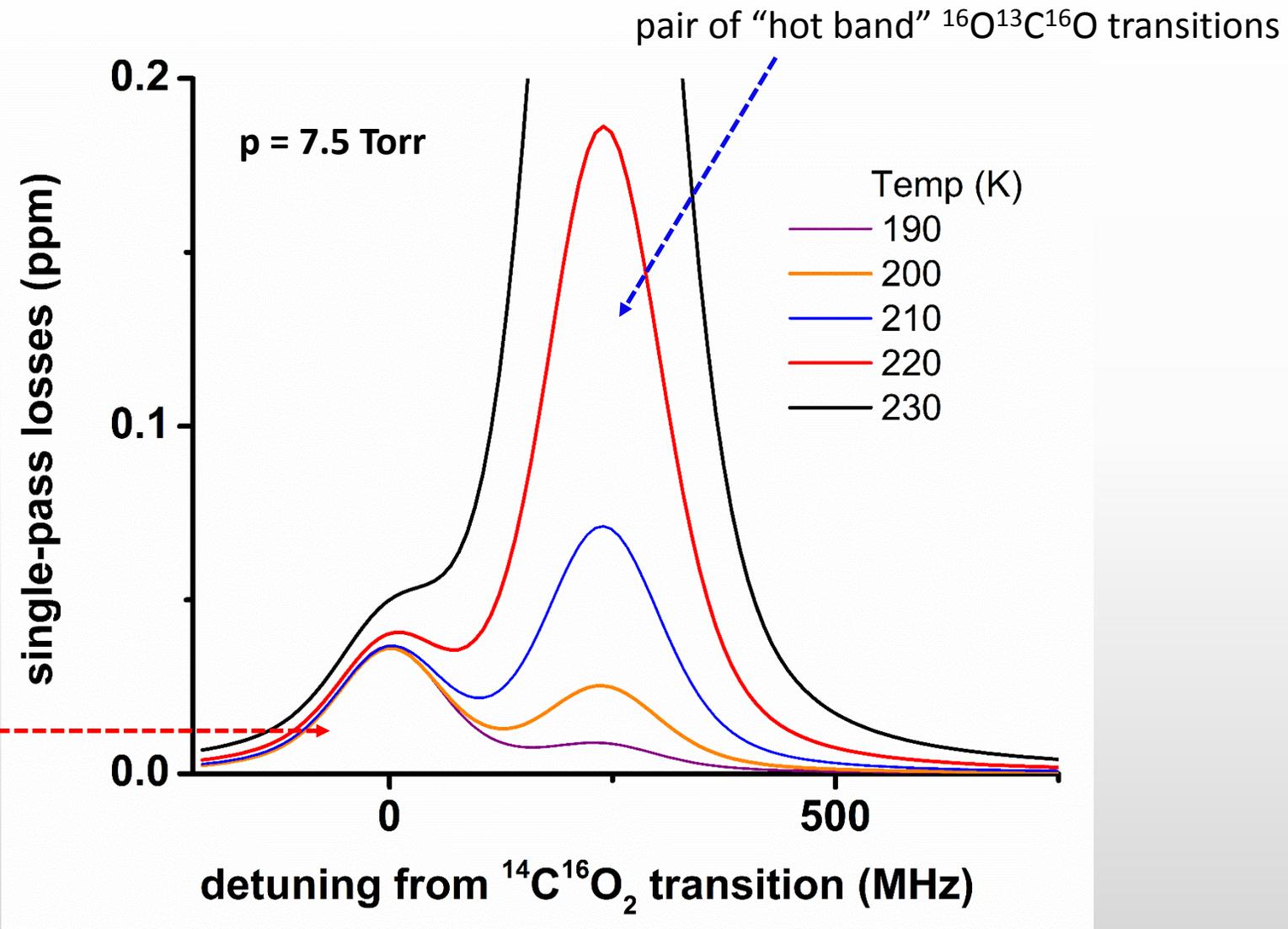
Quantum-noise-limited residuals in fitted decay signals



Calculated Absorption Spectra of Radiocarbon

Short-term precision of 0.0012 ppm
will give peak SNR of ~30:1

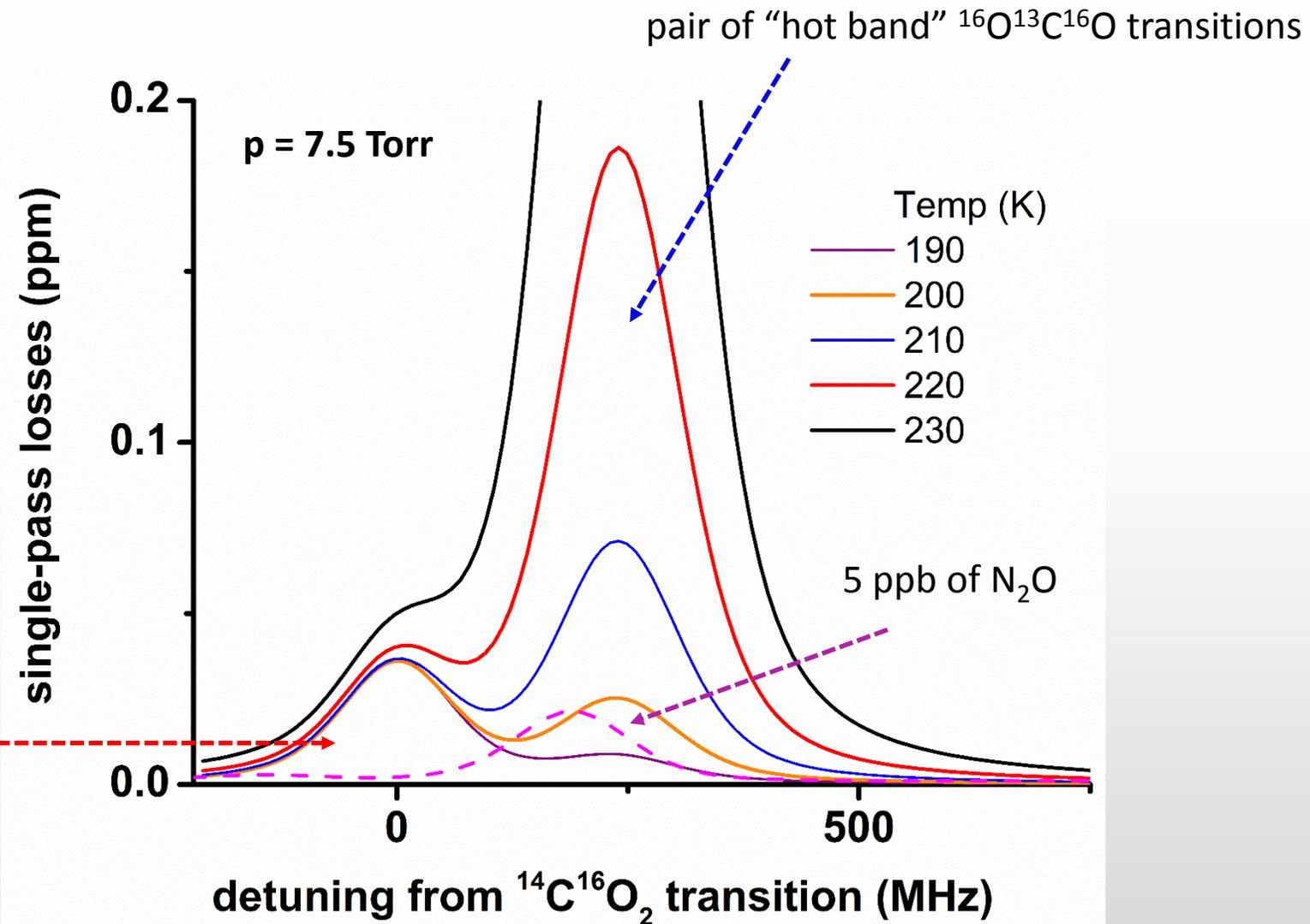
$^{16}\text{O}^{14}\text{C}^{16}\text{O}$ transition
at $\lambda = 4526.7137$ nm
1.2 parts-per-trillion



Calculated Absorption Spectra of Radiocarbon

N_2O desorption from walls is another interferent

$^{16}\text{O}^{14}\text{C}^{16}\text{O}$ transition
at $\lambda = 4526.7137$ nm
1.2 parts-per-trillion



Conclusions

SI-traceable measurements of concentration at (~ 0.2 % uncertainty level) over a range of p , T and mixture composition can be realized provided that
both the x and y axes of absorption spectra are acquired with high fidelity, and the absorber intensity is known from experiment or calculation.

This intrinsic standard approach is attractive for trace and reactive species as well as for rare isotopologues and for measurements of isotopic ratios.

Mid-IR QC laser, cavity-enhanced spectroscopy for the measurement of $^{14}\text{CO}_2$ provides a promising alternative to AMS-based methods.

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Guest Researchers

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California Institute of Tehnology



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NASA OCO-2 Science Team